

## Final Exam Review Math 150

- 1) Evaluate  $MR(x)$  for  $p(x) = -\frac{x}{10} + 3$  in dollars at the production level  $x = 25$
- 2) Determine the equation of the tangent line to  $f(x) = (3x - 2)^4$  at  $(1, 1)$
- 3) Find  $f'(x)$  if  $f(x) = 5x^3e^x$
- 4) Use implicit differentiation to find  $dy/dx$ :  $3x^2 + 5x + 8y^3 = 0$
- 5) Determine  $E(p)$  given  $d(p) = 1250 - p^2$  and price  $p = 5$
- 6) Determine any inflection points, as ordered pairs:  $f(x) = -x^3 + 9x^2 - 24x + 18$
- 7) Determine  $\int (5\sqrt{x} - 2x^{3/2})dx$
- 8) Find the area under  $f(x) = \frac{1}{\sqrt{x}}$  on  $[1, 4]$
- 9) Find the area bounded by:  $y = x + 2$  and  $y = x^2 - 4$
- 10) Given the supply function  $s(x) = 0.05x^2 + 15$  and the demand function  $d(x) = 2542 - 0.02x^2$  find the equilibrium point.
- 11) Given the supply function  $s(x) = 0.45x + 30$  and the demand function  $d(x) = -0.25x + 240$  find the consumer's surplus
- 12) Find  $f_x(1,2)$  given  $f(x,y) = (7x - 2y)^4$
- 13) Find  $f_{xy}(x,y)$  given  $f(x,y) = 5x^3y + xe^y$
- 14) Evaluate:  $\int_1^2 4x^3y^2dx$
- 15) Evaluate:  $\int_0^1 \int_0^2 (6x^2y - 9e^{2x}y) dx dy$  (keep answer exact!)

## Answers:

1)  $MR(25) = -2$

2)  $y = 12x - 11$

3)  $5x^3e^x + 15x^2e^x = 5x^2e^x(3+x)$

4)  $\frac{-6x-5}{24y^2}$  or  $-\frac{6x+5}{24y^2}$

5)  $E(p) = \frac{2p^2}{1250-p^2}$        $E(5) = 2/49 = 0.041$

6) Inflection point: (3,0)

7)  $\frac{10x^{3/2}}{3} - \frac{4x^{5/2}}{5} + c$

8) Area = 2

9) 125/6

10) (190, 1820)

11) \$11,250

12) 756

13)  $15x^2 + e^y$

14)  $15y^2$

15)  $\frac{369 - 81e^4}{4}$