Math 150
Chapter 4 Review
Find or Evaluate each Integral:

1) $\int 200 x^{4} d x$
2) $\int\left(\sqrt{x^{3}}+e^{x}+\frac{4}{x}\right) d x$
3) $\int_{0}^{6} e^{-5 x} d x$
4) $\int_{-1}^{2}\left(5 x+4 x^{3}\right) d x$

Find each Integral:
5) $\int t^{4}\left(t^{5}+6\right)^{3} d t$
6) $\int \sqrt{4 x^{2}+36} d x$
7) A cookie company determines its marginal cost of the $\mathrm{x}^{\text {th }}$ gourmet cookie to be: $c^{\prime}(x)=-0.0002 x+1.25$ where the cost to make 10 gourmet cookies is $\$ 17.49$.
a) Find the cost function $C(x)$
b) Use the cost function to determine the cost to produce 1000 cookies
8) Find the area under $y=5 x-x^{2}-6$ on $[2,3]$. Sketch and shade the area.
9) Find the area bounded by $f(x)=9-x^{2}$ and $g(x)=-x-3$. Include a sketch of the area.
10) Find the average value of $y=4 t^{3}+2 t$ over $[-1,2]$
11) A company estimates that its revenue will grow at a rate given by: $R^{\prime}(t)=3 e^{3 t}$. Where $\mathrm{R}^{\prime}(\mathrm{t})$ is the rate at which the revenue is increasing on the $t^{\text {th }}$ day. Find the total (accumulated) revenue for the first 4 days.

Answers:

1) $40 x^{5}+c$
2) $\frac{2}{5} \sqrt{x^{5}}+e^{x}+4 \operatorname{Ln} x+C$
3) $\frac{-1}{5 e^{30}}+\frac{1}{5}$
4) $45 / 2$
5) $\frac{\left(t^{5}+6\right)^{4}}{20}+C$
6) $x \sqrt{x^{2}+9}+9 \operatorname{Ln}\left|x+\sqrt{x^{2}+9}\right|+C$
7) a. $C(x)=-0.0001 x^{2}+1.25 x+5$
b. The cost to make 1000 cookies is $\$ 1155$
8) $1 / 6$
9) $343 / 6$
10) average value $=6$
11) the total revenue is approximately $\$ 162,753.79$
